



## Following Electron Impact Excitation of Single ( ${}_{30}\text{Zn}$ , ${}_{31}\text{Ga}$ , ${}_{32}\text{Ge}$ , ${}_{33}\text{As}$ , ${}_{34}\text{Se}$ , ${}_{35}\text{Br}$ , ${}_{36}\text{Kr}$ , ${}_{37}\text{Rb}$ , ${}_{38}\text{Sr}$ , ${}_{39}\text{Y}$ , ${}_{40}\text{Zr}$ ) atoms $L_i$ Subshell Ionization Cross Sections by using Lotz's Equations

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**Abstract:** L shell and three  $L_i$  sub shells ionization cross sections  $\sigma_L$  and  $\sigma_{L_i}$  following electron impact on ( ${}_{30}\text{Zn}$ ,  ${}_{31}\text{Ga}$ ,  ${}_{32}\text{Ge}$ ,  ${}_{33}\text{As}$ ,  ${}_{34}\text{Se}$ ,  ${}_{35}\text{Br}$ ,  ${}_{36}\text{Kr}$ ,  ${}_{37}\text{Rb}$ ,  ${}_{38}\text{Sr}$ ,  ${}_{39}\text{Y}$ ,  ${}_{40}\text{Zr}$ ) atoms calculated. By using Lotz's equation in Matlab ionization cross section values obtained for 20 electron impact energy  $E_{0i}$ . These values chosen in  $E_{L_{Li}} < E_{0i} < 10E_{L_{Li}}$  (first ionization energy  $E_{L_{Li}}$  to about  $14 E_{L_{Li}}$  to  $10,3 E_{L_{Li}}$ ; of ( ${}_{30}\text{Zn}$  to  ${}_{37}\text{Rb}$ ); and  $9,52 E_{L_{Li}}$  to  $7,55 E_{L_{Li}}$ ; of ( ${}_{38}\text{Sr}$  to  ${}_{40}\text{Zr}$ ) range for each atom. Lotz's parameters and special commands used for each ionization cross sections calculations. Starting all most from ionization threshold values; ionization cross sections are increasing rapidly with electron impact energy  $E_0$ . For higher  $E_0$  values this increments getting smaller for every  $L_i$  sub shells. For smaller  $E_0$  energy close to threshold; all ionization cross sections decrease. For a fixed electron impact energy while  $Z$  value increases from  $30 \leq Z \leq 40$ ; ionization cross sections decrease with  $Z$ . Results may help to understand similar findings which obtained from other electron impact excitation of  $L_i$  subshells ionization cross sections studies for similar size single atoms.

**Keywords:**  $L_i$  sub shells ionization cross section calculations, Electron impact on single atoms ( $30 \leq Z \leq 40$ ), Lotz's equations.

### 1. Introduction

Inner sub shell ionization cross section studies of free atoms by electron impact are subjects of ongoing research for many years [1,2,5-15]. Inner shell ionization cross section information help us to understand, characterization of used target atoms in the following fields: astrophysics, plasma physics, radiation protection, energy transfer by electron impact on or in tissues study required [5,6,7,8]. In this study, L shell and  $L_i$  sub shells ionization cross sections  $\sigma_L$  and  $\sigma_{L_i}$  ( $i=1,2,3$ ) for  ${}_{30}\text{Zn}$  to  ${}_{40}\text{Zr}$  atoms are calculated. For each of atoms, 20 electron impact energy values  $E_{0i}$  are used.  $E_{0i}$  ( $i=1, \dots, 20$ ) values were chosen in about the  $E_{L_{Li}} < E_{0i} < 10E_{L_{Li}}$  range for each atom.  $E_{L_i}$  is the binding energy of  $i^{\text{th}}$   $L_i$  ( $i=1, \dots, 3$ ) sub shells. If a neutral atom A bombarded by an electron with sufficiently big  $E_{0i}$  under  $E_{L_i} < E_{0i}$  conditions, firstly impacting electron emits bremsstrahlung then electron-single atom interaction occur. Target atom A becomes excited ions  $A^{*}$  at  $i^{\text{th}}$   $L_i$  sub shell. Creation of electron holes in  $L_i$  sub shells depends on how big the  $E_{0i}$  compare to  $E_{L_i}$ . Lotz put forward a semi-empirical formula at, for calculation of ionization cross sections for low energetic electron impact excitation of free atoms at inner shells which was based on Born Approximation (BA) [1,2,6]. Calculations for  $\sigma_L$  and  $\sigma_{L_i}$  ( $i=1,2,3$ ) of  ${}_{30}\text{Zn}$ ,  ${}_{31}\text{Ga}$ ,  ${}_{32}\text{Ge}$ ,  ${}_{33}\text{As}$ ,  ${}_{34}\text{Se}$ ,  ${}_{35}\text{Br}$ ,  ${}_{36}\text{Kr}$ ,  ${}_{37}\text{Rb}$ ,  ${}_{38}\text{Sr}$ ,  ${}_{39}\text{Y}$ ,  ${}_{40}\text{Zr}$  atoms carried out by using Lotz equations in Matlab program [7,9-12].

$$\sigma_{L_i} = a_{L_i} q_{L_i} [\ln(E_0/E_{L_i})/E_0 E_{L_i}] [1 - b_i \exp(-c_i (E_0/E_{L_i}))] \quad (1)$$

$a_{L_i}$ ,  $b_{L_i}$ ,  $c_{L_i}$  constants and  $q_{L_i}$  of the  $i^{\text{th}}$  sub shell which are taken from Lotz [1,2].  $q_{L_i}$  are the number of equivalent electrons at  $i^{\text{th}}$   $L_i$  sub shell and  $E_{L_i}$  is the binding energy of the  $i^{\text{th}}$  sub shell.  $\sigma_{L_i}$  are the ionization cross section of  $i^{\text{th}}$  sub shells. By using the Eq.1 and using sum of calculated  $\sigma_{L_i}$  sub shells of each atom for 20 values of  $E_{0i}$ ,  $\sigma_{L_{\text{total}}}$  of L shell calculated.

### 2. Method

L shell and  $L_i$  sub shells ionization cross sections  $\sigma_L$  and  $\sigma_{L_i}$  for  ${}_{30}\text{Zn}$  to  ${}_{40}\text{Zr}$  atoms are calculated. Calculations done for 20  $E_{0i}$  ( $i=1, \dots, 20$ ) values which they chosen in energy range of  $E_{L_{Li}} \leq E_{0i} \leq 10E_{L_{Li}}$  for each atom. It means that for  ${}_{30}\text{Zn}$ , used over all  $E_{0i}$  values fall in  $1,2\text{keV} < E_0 < 17\text{keV}$  range.  $E_{0i}$  values chosen according to the  $E_{L_{Li}}$  of targeted atom which were taken from Gwyn, and Porter [3, 4]. Calculations carried out by using written commands for Lotz's Eq.1 in Matlab for each atom [1,2,9 -14]. The values of  $a_{L_i}$ ,  $b_{L_i}$ ,  $c_{L_i}$  parameters and  $q_{L_i}$  are given in the same order for  $L_i$  sub shells as:

For  $a_{L_i}$  equal to  $(4, 2, 2) \cdot 10^{-14} \text{cm}^2 (\text{eV})^2$ ; for  $b_{L_i}$  equal to 0.5, 0.92, 0.92; for  $c_{L_i}$  equal to 0.6, 0.19, 0.19, and for  $q_{L_i}$  equal to 2, 2, 4, values used [1-2, 9-12]. By using the Eq.1 and using sum of calculated  $\sigma_{L_i}$  sub shells of each atom for 20 values of  $E_{0i}$ ,  $\sigma_{L_{\text{total}}}$  of L shell calculated.

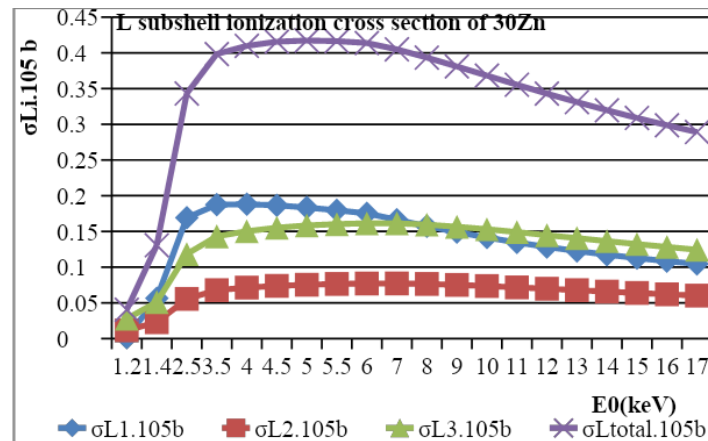


### 3. Results

Results for  $\sigma_L$  and  $\sigma_{L_i}(i=1,2,3)$  of  ${}_{30}\text{Zn}$  to  ${}_{40}\text{Zr}$  for 20  $E_{oi}$  are given in Table.1 to 11 under the name of each atom. Each table contains L sub shell ionization cross section results of one atom. All the Table captions are the same except the chemical symbol of elements which used for targeted atoms. Z dependency of ionization cross sections for a fixed  $E_{oi} = 10$  keV impact given in Table 12 and in Figure.12. Ionization cross section values are given in b(barn) units in tables and in all figures.

**Table.1** L subshell ionization cross section of  ${}_{30}\text{Zn}$  in  $10^5$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{L\text{total}} \cdot 10^5 \text{b}$
1,2	0,0013	0,0115	0,0277	0,0405
1,4	0,0565	0,0229	0,0512	0,1306
2,5	0,1692	0,0556	0,1183	0,3431
3,5	0,1874	0,0678	0,1432	0,3984
4	0,1881	0,0714	0,1503	0,4098
4,5	0,1866	0,0738	0,1552	0,4156
5	0,1835	0,0754	0,1584	0,4173
5,5	0,1796	0,0765	0,1603	0,4164
6	0,1753	0,0771	0,1614	0,4138
7	0,1663	0,0772	0,1614	0,4049
8	0,1574	0,0765	0,1595	0,3934
9	0,1491	0,0752	0,1566	0,3809
10	0,1415	0,0736	0,1531	0,3682
11	0,1346	0,0717	0,1491	0,3554
12	0,1283	0,0698	0,1448	0,3429
13	0,1226	0,0678	0,1407	0,3311
14	0,1175	0,0658	0,1364	0,3197
15	0,1127	0,0639	0,1323	0,3089
16	0,1084	0,062	0,1283	0,2987
17	0,1045	0,0602	0,1244	0,2891



**Figure.1** L subshell ionization cross section of  ${}_{30}\text{Zn}$  in  $10^5$  b.

**Table.2** L subshell ionization cross section of  ${}_{31}\text{Ga}$  in  $10^5$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{L\text{total}} \cdot 10^5 \text{b}$
1,3	0,0003	0,0097	0,0221	0,0321
2	0,1065	0,0334	0,0722	0,2121
2,5	0,1359	0,0431	0,0922	0,2712
3,5	0,1571	0,0544	0,1153	0,3268
4	0,1595	0,0577	0,1221	0,3393
4,5	0,1594	0,0602	0,1271	0,3467
5	0,1578	0,0619	0,1305	0,3502
5,5	0,1552	0,0631	0,1328	0,3511



6	0,1521	0,0639	0,1343	0,3503
7	0,1453	0,0646	0,1354	0,3453
8	0,1382	0,0644	0,1348	0,3374
9	0,1314	0,0637	0,1331	0,3282
10	0,1251	0,0627	0,1308	0,3186
11	0,1192	0,0614	0,1279	0,3085
12	0,1139	0,0601	0,1249	0,2989
13	0,109	0,0585	0,1217	0,2892
14	0,1045	0,0571	0,1185	0,2801
15	0,1004	0,0555	0,1152	0,2711
16	0,0966	0,0541	0,1121	0,2628
17	0,0931	0,0525	0,1089	0,2545

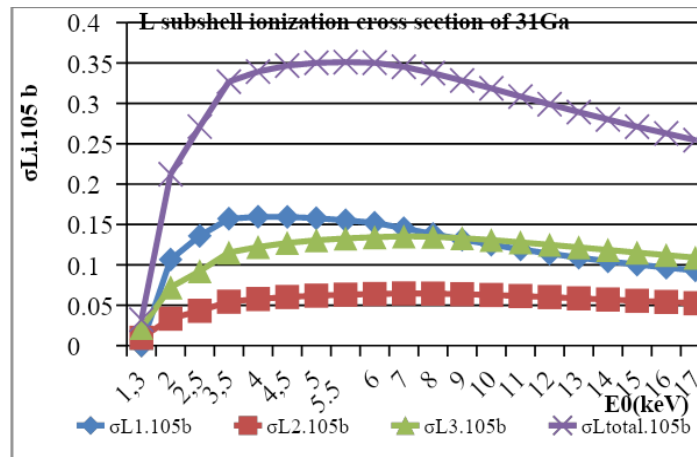


Figure.2 L subshell ionization cross section of  $^{31}\text{Ga}$  in  $10^5$  b.

Table.3 L subshell ionization cross section of  $^{32}\text{Ge}$  in  $10^5$  b

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{Ltotal} \cdot 10^5 \text{b}$
1,5	-0,0031	0,0068	0,0171	0,0208
2	0,0769	0,0243	0,0534	0,1546
2,5	0,1064	0,0331	0,0714	0,2109
3,5	0,1297	0,0434	0,0927	0,2658
4	0,1334	0,0466	0,0992	0,2792
4,5	0,1346	0,0491	0,1042	0,2879
5	0,1342	0,0507	0,1075	0,2924
5,5	0,1328	0,0521	0,1102	0,2951
6	0,1308	0,0529	0,1118	0,2955
7	0,1258	0,0539	0,1136	0,2933
8	0,1204	0,0542	0,1139	0,2885
9	0,1149	0,0539	0,1131	0,2819
10	0,1098	0,0533	0,1117	0,2748
11	0,1049	0,0525	0,1098	0,2672
12	0,1004	0,0515	0,1076	0,2595
13	0,0963	0,0505	0,1053	0,2521
14	0,0924	0,0493	0,1028	0,2445
15	0,0889	0,0481	0,1003	0,2373
16	0,0827	0,0458	0,0954	0,2239
17	0,0821	0,0452	0,0942	0,2215

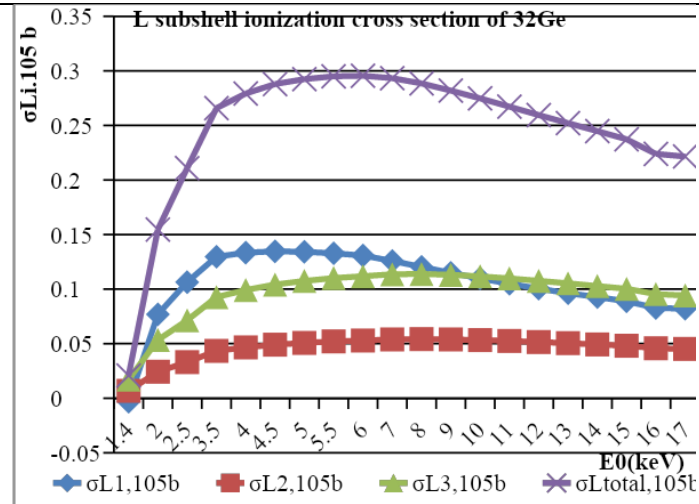


Figure.3 L subshell ionization cross section of  $^{32}\text{Ge}$  in  $10^5$  b

Table.4 L subshell ionization cross section of  $^{33}\text{As}$  in  $10^5$  b.

$E_0$ (keV)	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{Ltotal} \cdot 10^5 \text{b}$
1,5	-0,0045	0,0052	0,0138	0,0145
2	0,0546	0,0173	0,0386	0,1105
2,5	0,0838	0,0252	0,0549	0,1639
3,5	0,1085	0,0347	0,0744	0,2176
4	0,113	0,0377	0,0805	0,2312
4,5	0,1151	0,0399	0,0851	0,2401
5	0,1156	0,0416	0,0885	0,2457
5,5	0,1151	0,0429	0,0911	0,2491
6	0,1138	0,0439	0,0931	0,2508
7	0,1103	0,0451	0,0953	0,2507
8	0,1061	0,0456	0,0962	0,2479
9	0,1018	0,0457	0,0961	0,2436
10	0,0975	0,0454	0,0954	0,2383
11	0,0934	0,0449	0,0942	0,2325
12	0,0896	0,0442	0,0927	0,2265
13	0,0861	0,0435	0,0911	0,2207
14	0,0828	0,0427	0,0892	0,2147
15	0,0797	0,0418	0,0873	0,2088
16	0,0769	0,0409	0,0854	0,2032
17	0,0742	0,0401	0,0835	0,1978

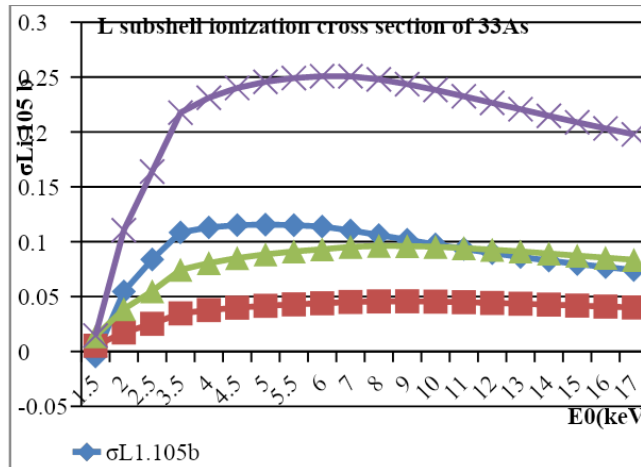


Figure.4 L subshell ionization cross section of  $_{33}\text{As}$  in  $10^5$  b.

Table.5 L subshell ionization cross section of  $_{34}\text{Se}$  in  $10^5$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{L\text{total}} \cdot 10^5 \text{b}$
1,5	-0,2213	0,0076	0,041	-0,1727
2	0,3509	0,1197	0,273	0,7436
2,5	0,6407	0,1912	0,4212	1,2531
3,5	0,8931	0,2776	0,5992	1,7699
4,5	0,9732	0,3264	0,6992	1,9988
5	0,9853	0,3428	0,7326	2,0607
5,5	0,9872	0,3555	0,7582	2,1009
6	0,9821	0,3654	0,7779	2,1254
6,5	0,9724	0,3729	0,7928	2,1381
7	0,9596	0,3786	0,8037	2,1419
8	0,9288	0,3855	0,8166	2,1309
9	0,8948	0,3882	0,8207	2,1037
10	0,8604	0,3879	0,8185	2,0668
11	0,8271	0,3854	0,8121	2,0246
12	0,7951	0,3813	0,8023	1,9787
13	0,7651	0,3762	0,7906	1,9319
14	0,7369	0,3703	0,7773	1,8845
15	0,7107	0,3639	0,763	1,8376
16	0,6862	0,3571	0,7482	1,7915
17	0,6634	0,3502	0,733	1,7466

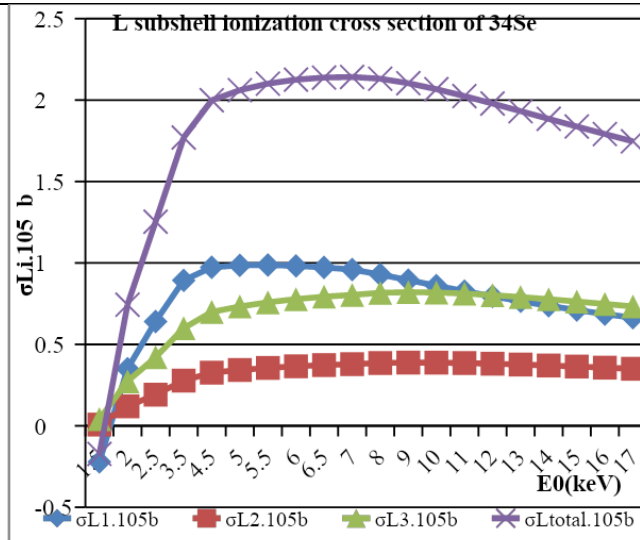


Figure.5 L subshell ionization cross section of  $^{34}\text{Se}$  in  $10^5$  b.

Table.6 L subshell ionization cross section of  $^{35}\text{Br}$  in  $10^5$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{Ltotal} \cdot 10^5 \text{b}$
1,6	-0,2141	0,0009	0,025	-0,1882
2,3	0,3833	0,1196	0,271	0,7739
2,9	0,6119	0,1799	0,3961	1,1879
3,6	0,7464	0,2269	0,4932	1,4665
4,75	0,833	0,2747	0,5915	1,6992
5,5	0,8477	0,2943	0,6313	1,7733
6	0,8481	0,3041	0,6509	1,8031
6,5	0,8437	0,3117	0,6662	1,8216
7	0,8359	0,3177	0,678	1,8316
8	0,8142	0,3257	0,6935	1,8334
9	0,7883	0,3299	0,7008	1,819
10	0,761	0,3313	0,7024	1,7947
11	0,7337	0,3306	0,6998	1,7641
12	0,7072	0,3284	0,6943	1,7299
13	0,6819	0,3252	0,6865	1,6936
14	0,658	0,3212	0,6772	1,6564
15	0,6355	0,3166	0,6667	1,6188
16	0,6144	0,3116	0,6556	1,5816
17	0,5947	0,3064	0,6439	1,545
18	0,5761	0,3009	0,6319	1,5089

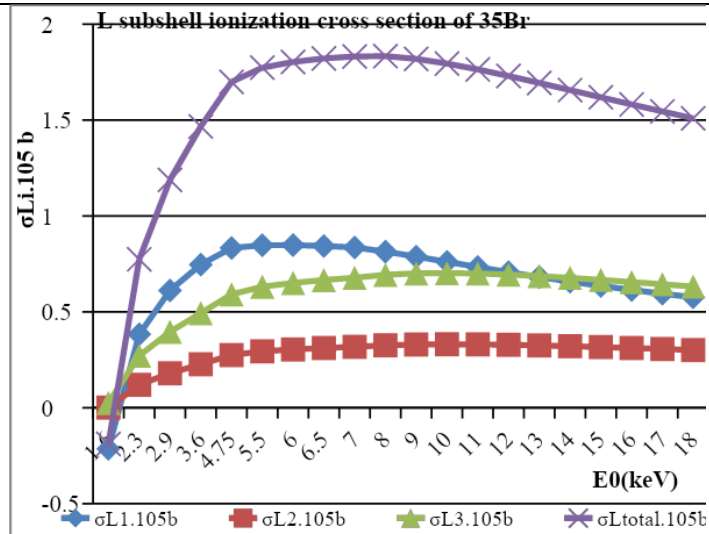


Figure.6 L subshell ionization cross section of  $^{35}\text{Br}$  in  $10^5$  b

Table.7 L subshell ionization cross section of  $^{36}\text{Kr}$  in  $10^5$  b

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{Ltotal} \cdot 10^5 \text{b}$
1,75	-0,1576	0,0035	0,0281	-0,126
2,4	0,2951	0,0922	0,2125	0,5998
3	0,4976	0,1432	0,3185	0,9593
3,7	0,6216	0,1836	0,4023	1,2075
4,75	0,7037	0,2228	0,4833	1,4098
5,5	0,7251	0,2414	0,5212	1,4877
6	0,7298	0,2508	0,5403	1,5209
6,5	0,7297	0,2584	0,5555	1,5436
7	0,7261	0,2644	0,5677	1,5582
8	0,7121	0,2731	0,5847	1,5699
9	0,6931	0,2783	0,5943	1,5657
10	0,6719	0,2809	0,5987	1,5515
11	0,6501	0,2816	0,5992	1,5309
12	0,6283	0,281	0,5968	1,5061
13	0,6073	0,2792	0,5923	1,4788
14	0,5871	0,2768	0,5863	1,4502
15	0,5682	0,2737	0,5792	1,4211
16	0,5499	0,2702	0,5709	1,391
17	0,5328	0,2663	0,5622	1,3613
18	0,5167	0,2623	0,5531	1,3321

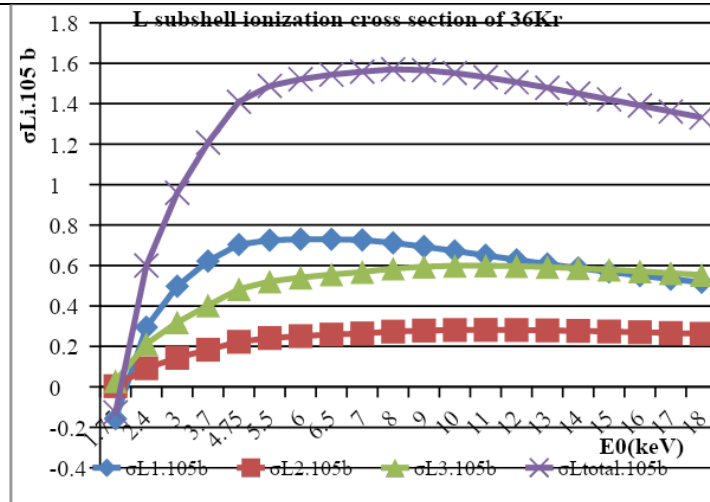


Figure.7 L subshell ionization cross section of  $_{36}\text{Kr}$  in  $10^5$  b

Table.8 L subshell ionization cross section of  $_{37}\text{Rb}$  in  $10^5$  b

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^5 \text{b}$	$\sigma_{L2} \cdot 10^5 \text{b}$	$\sigma_{L3} \cdot 10^5 \text{b}$	$\sigma_{Ltotal} \cdot 10^5 \text{b}$
1,85	-0,1631	-0,0021	0,0147	-0,1505
2,5	0,2246	0,0723	0,1696	0,4665
3,2	0,4257	0,1218	0,2726	0,8201
3,9	0,5299	0,1551	0,3418	1,0268
5	0,605	0,1894	0,4129	1,2073
5,9	0,6273	0,2078	0,4505	1,2856
6,5	0,6317	0,2168	0,4688	1,3173
7	0,6314	0,2228	0,4809	1,3351
8	0,6238	0,2317	0,4986	1,3541
9	0,6105	0,2374	0,5096	1,3575
10	0,5944	0,2408	0,5157	1,3509
11	0,5771	0,2425	0,5183	1,3379
12	0,5594	0,2428	0,5182	1,3204
13	0,542	0,2422	0,5161	1,3003
14	0,5251	0,2408	0,5124	1,2783
15	0,5089	0,2388	0,5075	1,2552
16	0,4934	0,2364	0,5017	1,2315
17	0,4787	0,2336	0,4953	1,2076
18	0,4648	0,2306	0,4884	1,1838
19	0,4516	0,2274	0,4812	1,1602

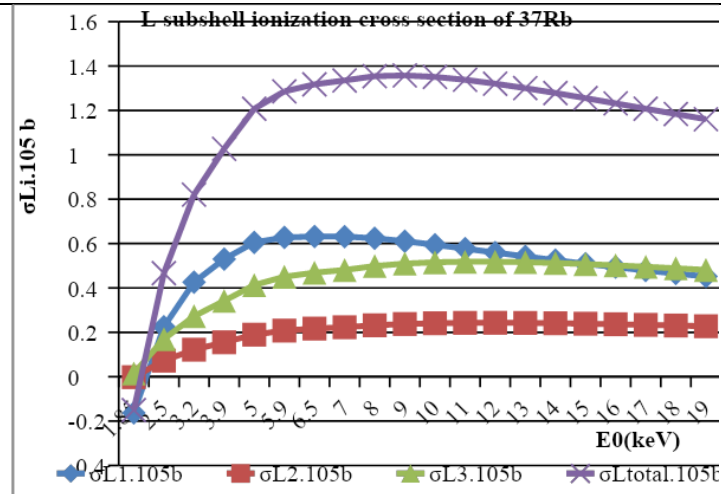


Figure.8 L subshell ionization cross section of  $_{37}\text{Rb}$  in  $10^5$  b

Table.9 L subshell ionization cross section of  $_{38}\text{Sr}$  in  $10^4$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^4 \text{b}$	$\sigma_{L2} \cdot 10^4 \text{b}$	$\sigma_{L3} \cdot 10^4 \text{b}$	$\sigma_{Ltotal} \cdot 10^4 \text{b}$
2,1	-0,0663	0,0106	0,0391	-0,0166
2,6	0,167	0,0557	0,1332	0,3559
3,5	0,3801	0,1075	0,2412	0,7288
4,4	0,4773	0,1399	0,3086	0,9258
5,3	0,5233	0,1618	0,3538	1,0389
6,2	0,5432	0,1771	0,3854	1,1057
7	0,5486	0,1871	0,4056	1,1413
8	0,5461	0,1959	0,4234	1,1654
9	0,5376	0,2019	0,4352	1,1747
10	0,5259	0,2058	0,4426	1,1743
11	0,5124	0,2081	0,4467	1,1672
12	0,4983	0,2093	0,4483	1,1559
13	0,484	0,2095	0,448	1,1415
14	0,47	0,2089	0,4462	1,1251
15	0,4563	0,2078	0,4432	1,1073
16	0,4431	0,2063	0,4394	1,0888
17	0,4305	0,2044	0,4349	1,0698
18	0,4185	0,2022	0,4298	1,0505
19	0,4071	0,1999	0,4244	1,0314
20	0,3962	0,1974	0,4186	1,0122

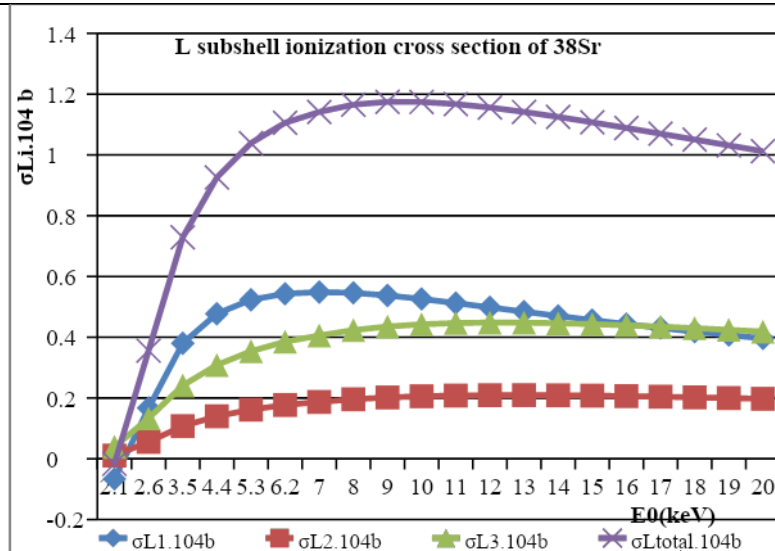


Figure.9 L subshell ionization cross section of  $_{38}\text{Sr}$  in  $10^4$  b.

Table.10 L subshell ionization cross section of  $_{39}\text{Y}$  in  $10^4$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^4 \text{b}$	$\sigma_{L2} \cdot 10^4 \text{b}$	$\sigma_{L3} \cdot 10^4 \text{b}$	$\sigma_{Ltotal} \cdot 10^4 \text{b}$
2,1	-0,1405	-0,0055	0,0042	-0,1418
2,4	0,0094	0,0212	0,0599	0,0905
2,8	0,1479	0,0487	0,1174	0,314
3,3	0,2614	0,0747	0,1718	0,5079
3,9	0,3471	0,0981	0,2205	0,6657
4,5	0,4002	0,1156	0,2573	0,7731
5	0,4292	0,1273	0,2816	0,8381
5,5	0,4489	0,1369	0,3015	0,8873
6	0,4618	0,1449	0,3179	0,9246
6,5	0,471	0,1516	0,3317	0,9543
7	0,4745	0,1572	0,3431	0,9748
7,5	0,4764	0,1619	0,3527	0,991
8,5	0,4746	0,1692	0,3674	1,0112
9	0,4718	0,1721	0,3729	1,0168
10	0,4638	0,1762	0,3811	1,0211
11	0,4538	0,1789	0,3862	1,0189
12	0,4428	0,1806	0,3891	1,0125
13	0,4313	0,1814	0,3901	1,0028
14,5	0,4141	0,1813	0,3891	0,9845
15,8	0,3995	0,1804	0,3863	0,9662

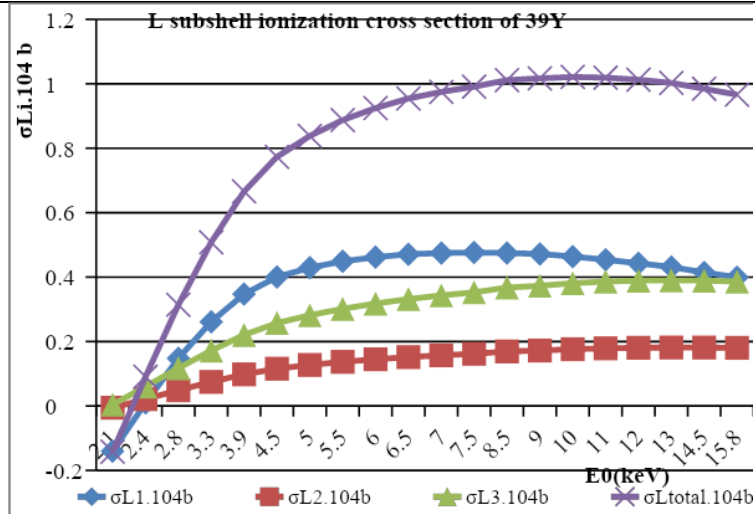


Figure.10 L subshell ionization cross section of  $_{39}\text{Y}$  in  $10^4$  b.

Table.11 L subshell ionization cross section of  $_{40}\text{Zr}$  in  $10^4$  b.

$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^4 \text{b}$	$\sigma_{L2} \cdot 10^4 \text{b}$	$\sigma_{L3} \cdot 10^4 \text{b}$	$\sigma_{Ltotal} \cdot 10^4 \text{b}$
2,25	-0,1172	-0,0045	0,0047	-0,117
2,5	-0,0116	0,0141	0,0434	0,0459
2,75	0,0702	0,0295	0,0759	0,1756
3	0,1348	0,0427	0,1036	0,2811
3,5	0,2285	0,0642	0,1484	0,4411
4,5	0,3344	0,0939	0,2108	0,6391
5	0,3642	0,1048	0,2333	0,7023
5,5	0,3851	0,1137	0,2519	0,7507
6	0,3995	0,1212	0,2675	0,7882
6,5	0,4092	0,1275	0,2805	0,8172
7	0,4153	0,1328	0,2915	0,8396
7,5	0,4188	0,1374	0,3007	0,8569
8,5	0,4201	0,1445	0,3152	0,8798
9	0,4188	0,1473	0,3208	0,8869
10	0,4137	0,1516	0,3294	0,8947
11	0,4063	0,1547	0,3352	0,8962
12	0,3977	0,1567	0,3388	0,8932
13,5	0,3837	0,1582	0,3413	0,8832
15	0,3694	0,1585	0,3412	0,8691
17	0,3508	0,1575	0,3381	0,8464

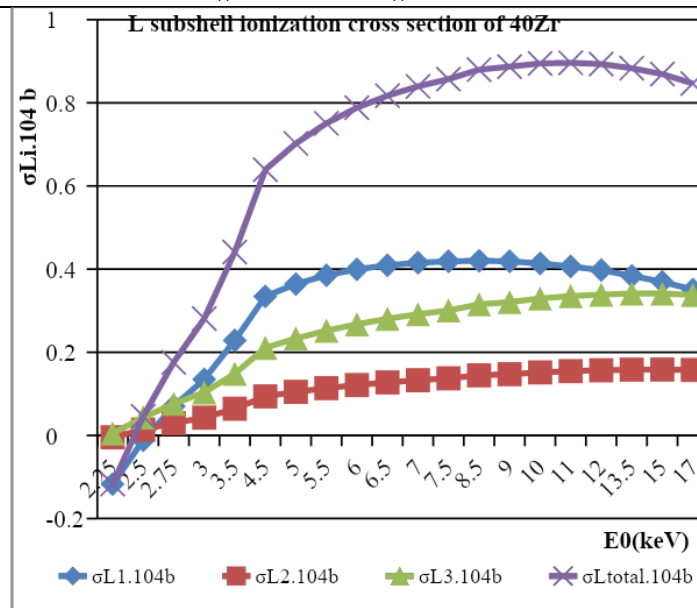


Figure.11 L subshell ionization cross section of  $^{39}\text{Zr}$  in  $10^4$  b.

Table.12 Z dependency of  $\sigma_{L_i}$  of  $^{30}\text{Zn}$  to  $^{40}\text{Zr}$  for 10keV electron impact in  $10^4$  b.

Atom No	$E_0(\text{keV})$	$\sigma_{L1} \cdot 10^4 \text{ b}$	$\sigma_{L2} \cdot 10^4 \text{ b}$	$\sigma_{L3} \cdot 10^4 \text{ b}$	$\sigma_{Ltotal} \cdot 10^4 \text{ b}$
30	10	14,151	7,362	15,311	36,824
31	10	12,511	6,271	13,081	31,863
32	10	10,98	5,331	11,172	27,483
33	10	9,749	4,539	9,541	23,829
34	10	8,604	3,879	8,185	20,668
35	10	7,61	3,313	7,024	17,947
36	10	6,719	2,809	5,987	15,515
37	10	5,944	2,408	5,157	13,509
38	10	5,259	2,058	4,426	11,743
39	10	4,638	1,762	3,811	10,211
40	10	4,137	1,516	3,294	8,947

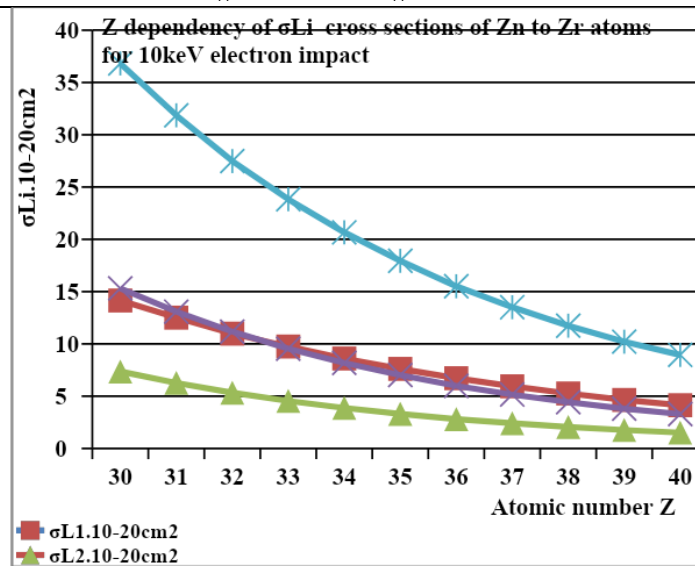


Figure.12 Z dependency of  $\sigma_{L_i}$  of  ${}_{30}\text{Zn}$  to  ${}_{40}\text{Zr}$  for 10keV electron impact in  $10^4$  b.

#### 4. Conclusions

L shell  $\sigma_L$  and  $\sigma_{L_i}$  sub shells ionization cross sections of  ${}_{30}\text{Zn}$ ,  ${}_{31}\text{Ga}$ ,  ${}_{32}\text{Ge}$ ,  ${}_{33}\text{As}$ ,  ${}_{34}\text{Se}$ ,  ${}_{35}\text{Br}$ ,  ${}_{36}\text{Kr}$ ,  ${}_{37}\text{Rb}$ ,  ${}_{38}\text{Sr}$ ,  ${}_{39}\text{Y}$ ,  ${}_{40}\text{Zr}$  by electron impact results given in Tabs.1 to 11 and in Figs.1 to 11. For L shell  $\sigma_L$  and for  $L_i$  sub shells  $\sigma_{L_i}$  increase rapidly by  $E_{0i}$  while  $E_{0i}$  increases from  $E_{L_{1i}} \leq E_{0i} \leq 10E_{L_{1i}}$  as shown in data Tables and at graphics in Figures. These increments of  $\sigma_L$  and of  $\sigma_{L_i}$  faster for very close to threshold energy values; increase by  $E_{0i}$  for data of each atom. Variation of  $\sigma_{L_i}$  by  $E_{0i}$  near to  $E_{L_i}$  region of  $L_i$  sub shells of each atom show similarity they are related to production of characteristic x ray yield rate of that sub shell.  $\sigma_{L_1}$  always for small values of  $E_{0i}$  crosses  $\sigma_{L_2}$  and  $\sigma_{L_3}$ . Then  $\sigma_{L_1}$  further gets bigger up to value of  $\sigma_{L_2}$  for highest electron impact energies and crosses again  $\sigma_{L_2}$  graphic for every atom. For a fixed  $E_{0i}=10$  keV, while Z value increases from  $30 \leq Z \leq 40$   $\sigma_L$  and  $\sigma_{L_i}$  decrease: Variation for  $\sigma_{L_{Total}}$  is from  $36,824.10^4$  b to  $8,947.10^4$  b. As seeing at Tab.12 and Fig.12,  $L_i$  sub shells  $\sigma_{L_i}$  ( $i=1,2,3$ ) decrease from 14,151b to 4,137b; 7,362b to 1,516b 15,311b to 3,294b respectively. Results must be compared with experimental measurements and with other calculations such as Distorted wave Born approximation (DWBA) and Modified Relativistic Bethe Born Approximations (MRBEB) [5-15].

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